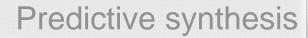






# Comments on Large-Scale Dynamic Predictive Regressions by Daniele Bianchi & Kenichiro McAlinn

Mike West





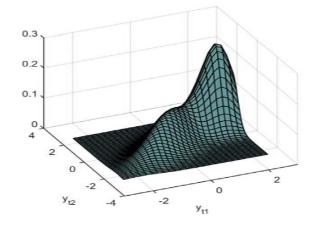
Forecast future time t: Vector outcome  $\mathbf{y}_t$ 

 $\mathcal{M}_1$   $\mathcal{M}_2$  • • •  $\mathcal{M}_j$  • • •

Model set:  $\mathcal{M}_{1:J}$ 

> Predictions:

 $h_{tj}(\mathbf{y}_t)$ 



Information:

$$\mathcal{H}_t = h_{t,1:J}(\cdot)$$

Predictive synthesis:  $p(\mathbf{y}_t | \mathcal{H}_t, \mathcal{I}_t)$ 

Past/prior information



$$p(\mathbf{y}_t|\mathcal{H}_t, \mathcal{I}_t) = \int_{\mathbf{X}_{t,1:J}} \alpha_t(\mathbf{y}_t|\mathbf{X}_{t,1:J}) \prod_{j=1:J} h_{tj}(\mathbf{x}_{tj}) d\mathbf{x}_{tj}$$

#### Synthesis model/pdf

(Dynamic) latent agent factors

- Model-specific biases, calibration
- Relative expertise/accuracy
- Model inter-dependencies
- Incomplete model set: Includes ability to "ignore" & adapt
- Time-variation ... in all the above
  - A subset of full Bayesian models (theory)
  - Many choices of synthesis model/function

[ Crosse & MW 1992; MW 1991,1992 ]

### Duke

#### A Few Comments on Bianchi & McAllin

Nice idea: Models to be synthesised = Subset regressions (dynamic)

MW1

- Uniform predictive improvements (over lasso, BMA, etc) why?
  - "illusion of sparsity" (high collinearities- avoid big models)
  - o don't select : mix over small models ... somehow
  - model set incompleteness: BPS "encompasses" and adapts
  - o dynamics
- Forecast goals focus: Build models for a purpose
  - multi-step or path-ahead forecast goals
  - o decision goals in other contexts
- Elucidates model/forecast interdependencies
  - o ... and their dynamics over time

#### Slide 4

MW1 prove

prove Mike West, 16/06/2018

#### A Few Connections



- Aggregation of "weak learners":
  - BART: ("boosting") McCulloch et al, 2010 AAOS
  - o Decision-guided SSS: MW et al 2004-10, JASA, JCGS
  - Lee & Clyde ("bagging") 2004 JMLR
- Emergent linked themes:
  - Shephard, Engle et al 2014 (bagging: "Composite likelihood" CL)
  - Chan, Koop et al 2018 CL for large TV-VARs
    - mixing large numbers of small intersecting models
    - structurally a special subclass of SGDLMs
- Decouple/Recouple: Rethinking modelling for scale-up SGDLMs: - decoupled sets of small univariate dynamic models
  - recoupled via (dynamic) simultaneous equations
  - G = graphical model underpinnings



#### Decouple/Recouple - SGDLMs

Vector outcome 
$$\mathbf{y}_t = (y_{1t}, \dots, y_{mt})'$$

$$y_{jt} \leftarrow \mathsf{DLM}(\mathbf{x}_{jt}, \mathbf{y}_{sp(j),t}, v_{jt})$$

Series *j* specific predictors

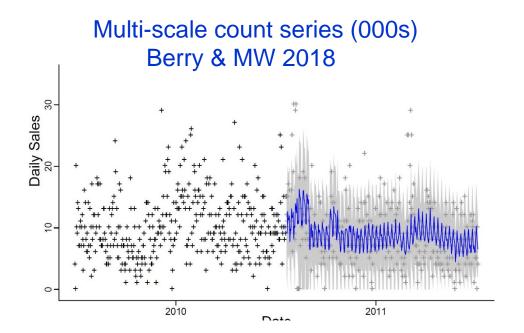
Simultaneous parental predictors

- Contemporaneous & lagged directed graphical models
- Flexible, sparse multivariate volatility structure induced
- Efficient forward filtering & forecasting
- Scale-up with m: Decouple/recouple analysis O(m)
- Examples: m ~ 400
- GPU implementation exemplar

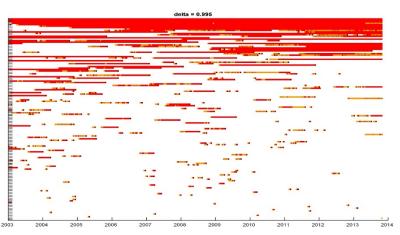
[ Lutz Gruber & MW; BA 2016, EcoStat 2017, + ...]

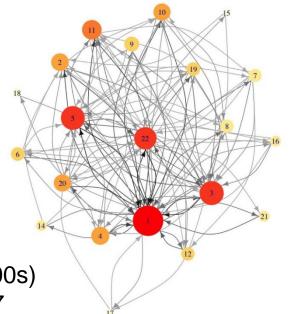


#### Decouple/Recouple for Large Time Series



#### SGDLMs - finance/macro econ (00s)





Dynamic network flows (000s) Xi, MW et al, JASA 2017

## Duke

### Bianchi & McAllin and DPR: A Few Questions

- Sum-to-one weights issue irrelevant! (e.g., all ~ 0)
- How to choose small models?
  - theory/insights/economics
  - o more details please
  - o "overlay" with statistical ideas? Parsimony: "orthogonal" models?
- Go deeper with model interdependencies
  - changes over time: utility in informing interventions?
  - generating insights for model set refinements?
- Predictive improvements:
  - Time-varying BPS parameters: Role of dynamics

#### A Few More Questions



- Macro example (eg): 8 models to be synthesised
  - DLMs with "too many" predictors- stability? Sparser models
  - o New thoughts: Hierarchical BPS ...?
- Key issues: multi-step ahead predictions
  - Univariate models require future values of predictors
  - Predict the predictors offline? (no mention in draft ....)
- Impulse response analysis & multi-step forecasting (for decisions)
  - Need multivariate models
  - SGDLM-DPR models Univariate DPRs coupled in SGDLM?